

Dokuz Eylül University, Department of Mathematics

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MATH 223 LINEAR ALGEBRA

Quiz 2

12.10.2004

Name

Student No.

Sign

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*You will not get any points if your answer is wrong, that is no points to your explanations if your answer is wrong. And of course no points to a correct answer if your explanation or proof is not correct or clear.*

*YOU must write GOOD Mathematics*

1. Let  $V = \mathbb{P}_2$  and  $T$  be the linear operator on  $V$  defined by  $T(f(x)) = (1 + x^2)f''(x) + f'(x) + f(x)$ .
  - (a) Find the characteristic polynomial and the eigenvalues of  $T$ .
  - (b) If possible, find a basis for  $\mathbb{P}_2$  consisting of eigenvectors of  $T$ .

*Solution:*